

# A New Look to THz Wireless Links: Fading Modeling and Capacity Assessment

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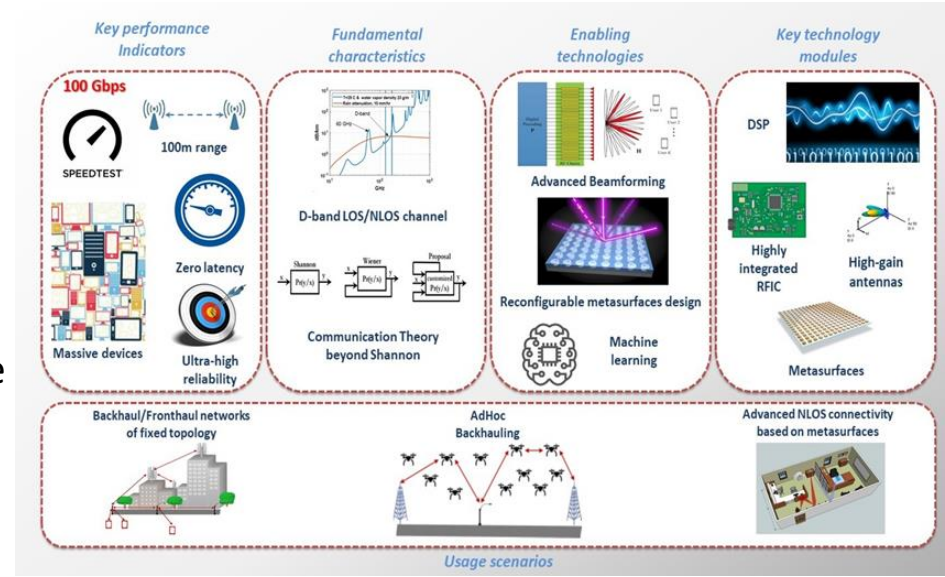
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# Motivation

Systems beyond 5G are expected to:

- Provide unprecedented performance excellence, in the 100 Gbps regime.
- Support novel usage scenarios combining extreme data rates with agility, reliability and zero response time.
- Exploit frequencies above 100 GHz.
- The THz band (0.1-10 THz) offers a vast amount of unallocated bandwidth.
- Is envisioned to sustain flexible and ubiquitously available networks for backhaul and access applications.



# Objective

- To investigate the small-scale fading statistics of THz wireless channels.
- Perceive a fading distribution that is not only analytically tractable, but also accurately describes the THz channels.
- Examine the suitability of  $\alpha - \mu$  distribution to model the small-scale fading of THz channels.
- Verify the accuracy of  $\alpha - \mu$  fitting to the empirical channel gain distributions of various indoor links measured at 142 GHz.
- Present the ergodic capacity performance of THz links under different levels of small-scale fading intensity.



# The $\alpha - \mu$ fading distribution

- The  $\alpha - \mu$  is a well-known fading distribution.
- It includes many well-known distributions, by appropriately setting  $\alpha$  and  $\mu$  values.
- The probability density function (PDF) of  $\alpha - \mu$  is expressed as

$$f(x) = \frac{\alpha \mu^\mu \left(\frac{x}{\beta}\right)^{\alpha \mu - 1} \exp\left(-\mu \left(\frac{x}{\beta}\right)^\alpha\right)}{\beta \Gamma(\mu)}$$

- For a random variable  $X$  following  $\alpha - \mu$

$$\beta = \sqrt[\alpha]{\mathbb{E}(X^\alpha)}$$

$$\mu = \frac{\mathbb{E}^2(X^\alpha)}{V(X^\alpha)}$$



## Capacity of $\alpha - \mu$ fading channels

- For a single-input-single-output (SISO) THz wireless system by assuming  $\alpha - \mu$  small-scale fading, the ergodic capacity is expressed as

$$C = \frac{\alpha \mu^\mu \left( \frac{\sqrt{1/\kappa}}{\beta} \right)^{\alpha \mu}}{2 \ln(2) \Gamma(\mu)} H_{3,4}^{4,1} \left[ \mu \left( \frac{\sqrt{1/\kappa}}{\beta} \right)^\alpha \left| \begin{matrix} \left( -\frac{\alpha \mu}{4}, \frac{\alpha}{4} \right), \left( 1 - \frac{\alpha \mu}{4} \right), & (1,1) \\ (0,1), & (1,1) & \left( -\frac{\alpha \mu}{4}, \frac{\alpha}{4} \right), \left( -\frac{\alpha \mu}{4}, \frac{\alpha}{4} \right) \end{matrix} \right. \right]$$

$$\kappa = \frac{P_t}{N_o} \frac{c G_t G_r}{16 \pi^2 f^2 d^2} \tau(f, d)$$

- Where  $H_{3,4}^{4,1}[\cdot]$  is the Fox-H function.

# Experimental Setup

- Indoor multipath measurements in the premises of a university.
- Two line-of-sight (LoS) links.
- Ten non-line-of-sight (NLoS) links.
- The transmitter (TX) and the receiver (RX) were static.
- No people were present during the measurements.
- A different link was defined by changing the TX position.



# Preprocessing of the measurement data

- The channel sounding yields power-angular-delay-profiles (PADP) for each TX-RX link.

$$PADP(\phi, t) = \sum_{i=1}^I G_a P_i \delta(\phi - \phi_i) \delta(t - t_i)$$

- To investigate the stochastic behavior of the THz channels, the deterministic pathloss must be omitted.

$$\zeta_i^2 = \frac{P_i}{\frac{\sum_{i=1}^I P_i}{I}}$$

- Where  $\zeta_i$  is the normalized path amplitude.



# Generation of different channel realizations

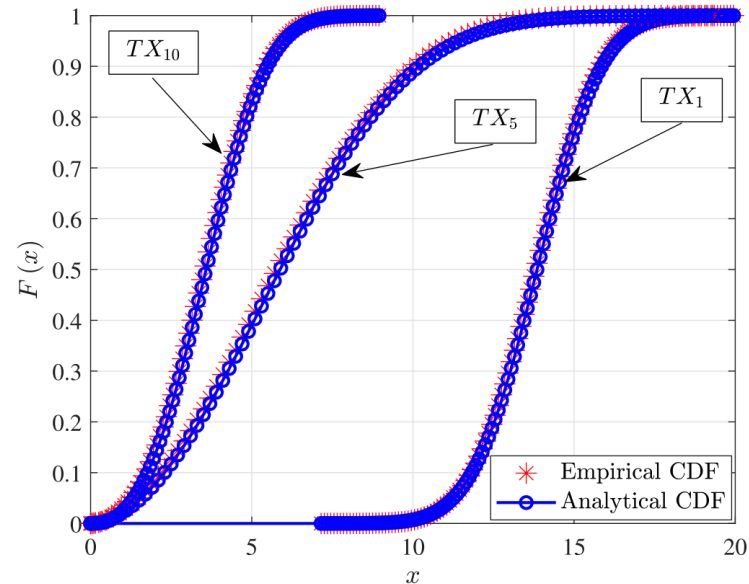
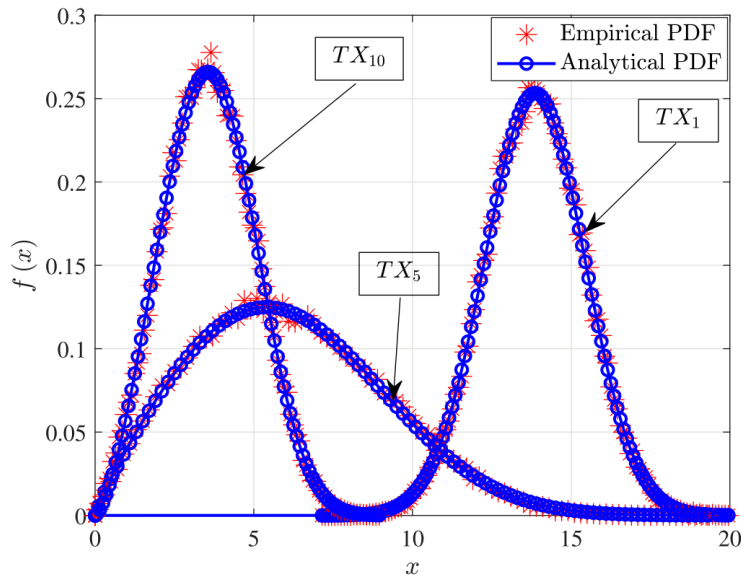
- The THz wavelengths are much smaller compared to the size of objects.
- The multipath richness is reduced.
- Different transfer function realizations can be generated by changing the phases of the multipath components.

$$h = \sum_{i=1} \zeta_i \exp(-j 2\pi f t_i) \exp(j\psi_i)$$

- By assuming a flat-fading channel,  $t_i = 0$ .

# Fitting of $\alpha - \mu$ to the empirical channel gain distributions (1/2)

- The  $\alpha - \mu$  fading distribution was found to adequately fit the empirical channel gain distributions of the measured links.
- The goodness of fit was evaluated in terms of the Kolmogorov-Smirnov test with a significance level of 5%.



# Fitting of $\alpha - \mu$ to the empirical channel gain distributions (2/2)

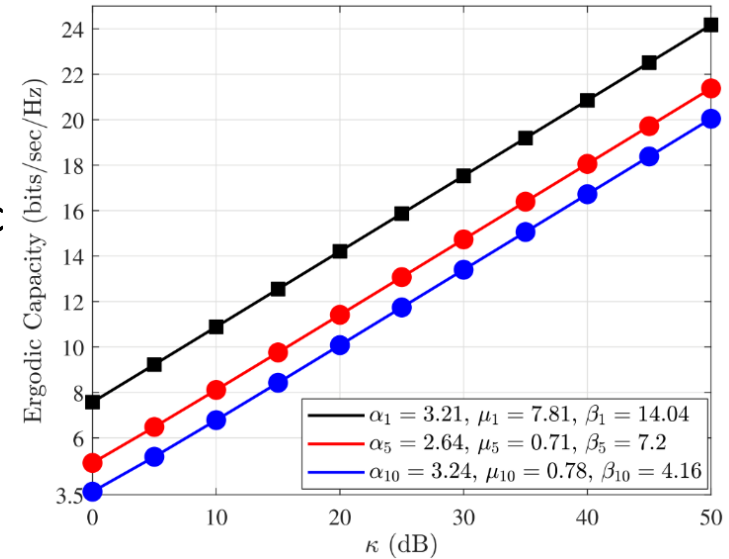
- $\alpha - \mu$  accurately fits the empirical channel gain distributions of both LoS and NLoS links.
- For the LoS links  $\mu > 1$ , while for the NLoS links  $\mu < 1$ .
- For both LoS and NLoS  $\alpha \in [2 - 3.25]$  except for link 4.

TX	$d$ (m)	$\alpha$	$\mu$	$\beta$	KS-test	LOS
1	4.35	3.21	7.81	14.04	✓	✓
2	9.82	3.13	3.76	11.36	✓	✓
3	3.3	3	0.66	10.77	✓	✗
4	17.01	8.55	0.23	8.5	✓	✗
5	11.24	2.64	0.71	7.2	✓	✗
6	23.31	2.48	0.78	7.27	✓	✗
7	28.71	2.48	0.77	3.65	✓	✗
8	20.16	-	-	-	✗	✗
9	30.65	2.29	0.85	6.35	✓	✗
10	47.44	3.24	0.78	4.16	✓	✗
11	12.59	-	-	-	✗	✗
12	10.19	3.25	0.72	3.05	✓	✗



# Capacity Evaluation

- The ergodic capacity of a SISO THz wireless link is evaluated for different values of  $\alpha$ ,  $\mu$  and  $\beta$ .
- For a given set of values, as  $\kappa$  increases the ergodic capacity improves.
- The increase of  $\kappa$  leads to pathgain and received power improvement.
- The ergodic capacity of link 1 is greater compared to links 5 and 10.
- Because  $\mu_5$  and  $\mu_{10}$  have similar values while  $\mu_1$  is greater.
- Also,  $\beta_1 > \beta_5 > \beta_{10}$ .



## Conclusions

- The small-scale fading statistics of THz wireless channels was investigated.
- For the first time the  $\alpha - \mu$  was fitted to experimentally obtained THz channel gain measurements.
- The  $\alpha - \mu$  achieves an adequate fit to the empirical channel gain distributions.
- More channel measurements are needed to identify the range of  $\alpha - \mu$  parameters to describe different indoor environments.



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- Site: <https://www.ict-ariadne.eu/>

